

**OLLSCOIL NA hÉIREANN, CORCAIGH**  
THE NATIONAL UNIVERSITY OF IRELAND, CORK

COLÁISTE NA hOLLSCOILE, CORCAIGH  
UNIVERSITY COLLEGE, CORK

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**SUMMER EXAMINATIONS, 2005**

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**B.E. DEGREE (ELECTRICAL)**

APPLIED POWER ELECTRONICS AND MOTION CONTROL  
EE4001

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Dr. J.G. Hayes

Time allowed: *3 hours*

Answer *four* out of six questions.  
All questions carry an equal weighting of 20 marks.

The use of a Casio fx570w or fx570ms calculator is permitted.

**1. Induction Motor Characterization**

- (a) The specification table for Westinghouse induction motors is provided as an attachment (see page 6). Consider the 110 kW, four-pole machine with 400 V (line-line), 50 Hz applied in the delta configuration. Assume  $R_S = 58.3 \text{ m}\Omega$ .
- (i) Determine the slope of the torque/speed (Nm/Hz) curve in its linear region?
  - (ii) Estimate the per-phase equivalent circuit parameters:  $L_M$ ,  $R_R'$ , and  $P_{CFW}$ .

[12 marks]

- (b) The four-pole, 22 kW induction motor in the tables is missing the power factor for the 50 % load point. Calculate an approximate value for the power factor based on the information provided at the 100 % load point.

[4 marks]

- (c) Given that the four-pole, 22kW motor has  $R_R' = 0.44 \Omega$  and  $R_S = 0.58 \Omega$ , determine the leakage inductances  $L_{LS}$  and  $L_{LR}'$ . Assume that  $L_{LR}' = \frac{3}{2} L_{LS}$  for this class of machine.

[4 marks]

## 2. Induction Motor Inrush and Speed Control

- (a) Sketch the wiring diagram of the star-delta starter for inrush control of the induction machine.

[3 marks]

- (b) The specification table for Westinghouse induction motors is provided as an attachment (see page 6). Consider the 22 kW, four-pole machine with 400 V (line-line), 50 Hz applied. What is the direct-on-line starting current when a star-delta starter is used?

[3 marks]

- (c) A four-pole star-connected motor outputs 40 Nm at 1746 RPM when supplied by a 60 Hz line-line voltage of 440 V and a phase current of 10.39 A lagging at a power factor of 0.866. The series resistance is 1.5  $\Omega$ .

(i) By maintaining a constant field flux, what are the electrical line voltage, current, frequency, and power factor sourced from the inverter, when developing 50% of the rated torque at 50% of the rated speed?

(ii) Determine values for the slip frequency, line current and power factor required to ensure constant-power operation of the machine at twice the rated speed.

Use the formula  $slope = \frac{V_{ph,rated} - R_S \cdot I_{R,rated}}{f_{rated}}$  for low-voltage boost.

[14 marks]

## 3. AC Machines Space Vectors and Vector Control of the Induction Motor

- (a) A 4-pole, 3-phase induction motor has the following physical dimensions: radius  $r = 6$  cm, length  $l = 24$  cm, airgap length  $l_g = 0.5$  mm, and number of turns per phase per pole  $N_{sp} = 50$ . The motor is supplied by a rated voltage of 400 V (line to line) at a frequency of 50 Hz.

(i) Calculate the per-phase magnetizing inductance and the per-phase magnetizing current of the machine.

(ii) Determine the magnitudes of the following rotating stator space vectors: current, voltage and flux density.

(iii) Determine the per-phase current and output torque when a per-phase reflected current  $I'_r = 5$  A flows in the stator.

[6 marks]

- (b) In a 4-pole induction machine, a per-phase current of 106.1 Arms at an input electrical frequency of 50 Hz is required to establish the rated airgap flux density. A per-phase current of 225 Arms at an input electrical frequency of 51.5 Hz is required to establish rated motoring torque at a mechanical rotor speed of 1500 rpm.
- Calculate the magnitudes of the space-vector current  $I_{ms,pk}$ , the stator direct-axis current  $i_{sd}$  and quadrature-axis current  $i_{sq}$ , and the three phase currents,  $i_a$ ,  $i_b$ , and  $i_c$ , to establish the rated flux at  $t = 0^-$ , the instant just before injection of a step current to develop rated torque.
  - Recalculate the above currents required to establish the rated flux and a *regenerative* torque at  $t = 0^+$ .
  - Assuming that the generator speed is constant at 1500 rpm, calculate the input electrical frequency and the per-phase currents at  $t = 5$  ms.

[14 marks]

#### 4. Power Electronics Converters

- (a) The Toyota Prius uses a 20 kW bidirectional converter to generate a 500 V dc link voltage from the 200 V NiMH battery. This higher voltage allows the efficiency, range, and emissions of the vehicle to be optimized. The bidirectional converter has an inductance of 435  $\mu$ H and switches at 10 kHz. The vehicle is operating in motoring mode and the bi-directional converter is required to act as a boost and provide a half power level of 10 kW. For this 10 kW condition:
- Calculate the rms currents in the inductor and in the output and input capacitors.
  - Calculate the switch average and rms currents and the resulting conduction losses in
    - the IGBT with  $V_{CE(knee)} = 2.5$  V and  $R_{CE} = 0.01$   $\Omega$ , and
    - the diode with  $V_{F(knee)} = 1.5$  V and  $R_F = 0.005$   $\Omega$ .

[12 marks]

- (b) The system parameters of a permanent-magnet dc motor supplied by a switch-mode PWM dc-dc converter are as follows: armature resistance  $R_a = 0.1$   $\Omega$ , armature inductance  $L_a = 1$  mH, motor constant  $k = 0.07$  V/(rad/s), dc bus voltage  $V_d = 12$  V, switching frequency  $f_s = 20$  kHz, and amplitude of triangular waveform control voltage  $V_{tri} = 5$  V. The motor is spinning forward at a speed of 750 rpm and acts as a *generator* supplied by a full-load torque of -0.7 Nm.
- Calculate the following: (a) the applied armature voltage  $V_{AB}$ ; (b) duty ratios for the overall converter, pole A, and pole B; (c) the control voltage, and (d) the peak-to-peak ripple on the armature current.
  - Calculate the rms currents in the upper and lower MOSFET switches of pole A.

[8 marks]

## 5. Power Semiconductors

- (a) Sketch the symbol and the vertical structure of the IGBT. Briefly state the advantages of the IGBT over the MOSFET for low frequency operation.

[5 marks]

- (b) The IRFPS40N60K power MOSFET (see attached specification sheets on pages 7 to 10) from International Rectifier operates in a boost converter with a dc link voltage  $V_d = 480$  V, and load current  $I_o = 20$  A. The MOSFET is driven by a gate drive IC outputting a square-wave voltage  $v_{GG}$ , of amplitude 0 V to +10 V, in series with an external gate resistance  $R_G = 4.3 \Omega$ . Assume the diode has a 1V forward drop and no reverse recovery.

Useful formula: RC discharge time  $t = -RC \ln \left[ \frac{v_c - (-V_{GG})}{V_{ci} - (-V_{GG})} \right]$

- (i) Determine the following parameters from the data sheet at a junction temperature of 100°C: maximum threshold voltage, minimum forward transconductance, gate-source capacitance, gate-drain capacitance, maximum on-state resistance, maximum gate voltage at the 20 A load current, and maximum conduction drop across MOSFET at 20 A.
- (ii) Sketch  $v_{GG}(t)$ ,  $v_{GS}(t)$ ,  $v_{DS}(t)$ , and  $i_D(t)$  during turn-off of the MOSFET. Note the approximate voltage levels on waveforms.
- (iii) Calculate the following (a) turn-off delay time  $t_{doff}$ , (b) voltage rise time  $t_{vr}$ , and (c) current fall time  $t_{fv}$  at a junction temperature of 100°C. Sketch the basic switching circuit under analysis in each case.
- (iv) Calculate the turn-on off energy loss.

[15 marks]

## 6. DC Machines

- (a) A motor/generator with a pure inertial load is often used as a flywheel to store energy. A motor has a machine constant of  $0.5 \text{ Nm/A}$ , an armature resistance of  $0.35 \text{ } \Omega$ , and an inertia  $J = 0.06 \text{ kg m}^2$ . Calculate the electrical energy recovered when the machine slows from  $1500 \text{ rpm}$  to  $750 \text{ rpm}$ . The braking current is clamped at  $10 \text{ A}$  during the energy recovery period.
- [8 marks]
- (b) A  $100 \text{ kW}$  compound generator, of terminal ratings  $250 \text{ V}$  and  $400 \text{ A}$ , has an armature resistance (including brushes) of  $0.025 \text{ } \Omega$  and the attached magnetization curve (see page 11). There are  $1000$  shunt-field turns per pole and  $3$  series-field turns per pole. Compute the shunt field current required at full load when the generator speed is  $1100 \text{ rpm}$ . Include the effects of armature reaction.
- [6 marks]
- (c) A magnetic circuit consists of a high permeability core, an airgap of length  $l_g = 1 \text{ mm}$  and cross-sectional area  $A_g = 100 \text{ cm}^2$ , and a rare-earth Nd-Fe-B permanent magnet with the attached magnetization curve (see page 11).
- (i) Determine the point of maximum energy density for the magnet.
  - (ii) Find the minimum magnet volume required to achieve an airgap flux density of  $0.8 \text{ T}$ .

[6 marks]